
Satz: $f :]a, b[\Rightarrow \mathbb{R}, c \in]a, b[$, so daß $f'(c)$ existiert. Dann ist f auch stetig in c .
Bew: zz:

$$\lim_{x \rightarrow c} f(x) = c$$

$$\left(\lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c} = \lim_{x \rightarrow c} = 0 \Rightarrow 0 = \lim_{x \rightarrow c} \frac{f(x) - f(c)}{x - c} \cdot (x - c) = \lim_{x \rightarrow c} (f(x) - f(c)) \Rightarrow \lim_{x \rightarrow c} f(x) = f(c) \right)$$

$$f'(c) + g'(c) = \lim_{x \rightarrow c} \left(\frac{f(x) - f(c)}{x - c} + \frac{g(x) - g(c)}{x - c} \right) = \lim_{x \rightarrow c} \left(\frac{f(x) + g(x) - (f(c) + g(c))}{x - c} \right) = \lim_{x \rightarrow c} \frac{(f + g)(x) - (f + g)(c)}{x - c}$$